

# Visual-Inertial Odometry with Point and Line Features

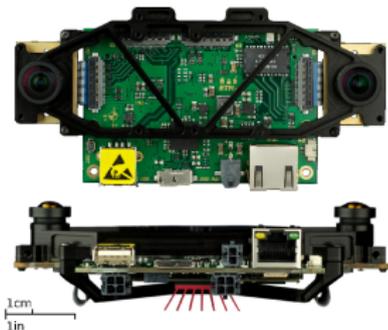
---

Yulin Yang, Patrick Geneva, Kevin Ekenhoff and Guoquan Huang  
November 15, 2019

University of Delaware, Newark DE, USA

# Introduction

- Visual-inertial navigation is widely used for 6DOF estimation.
- Rich amount of geometrical information available in man-made environment can be exploited.
- Points and lines are most commonly seen and can both be utilized for robust and accurate pose estimation.



- A tightly-coupled monocular visual-inertial navigation system which leverages point&lines and is evaluated on real-world datasets.
- Discuss two 3D line feature triangulation algorithms.
- Degenerate motion identification for 3D line triangulation based on line segment measurements.
- Performance evaluation for 3 line representations in a visual SLAM scenario.

- Kottas et al. [1] proposed to use lines in VIO with quaternion representation and performed line obs analysis.
- Guo et al. [2] utilized SLAM line (free&structural) within a visual-inertial SLAM system.
  - No degenerate motion analysis.
  - Only use only quaternion to represent line orientation.
- Yu et al. [3] proposed two point inverse depth parameterization and applied line feature for rolling shutter.
  - No degenerate motion analysis.
  - No comparisons of line triangulation algorithms.

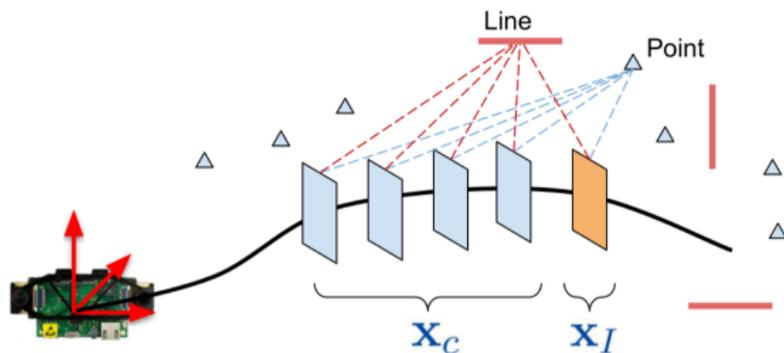
---

[1] Kottas and Roumeliotis, "Efficient and consistent vision-aided inertial navigation using line observations"

[2] Guo et al., "Large-scale cooperative 3d visual-inertial mapping in a manhattan world"

[3] Yu and Mourikis, "Vision-aided inertial navigation with line features and a rolling-shutter camera"

# Problem Formulation



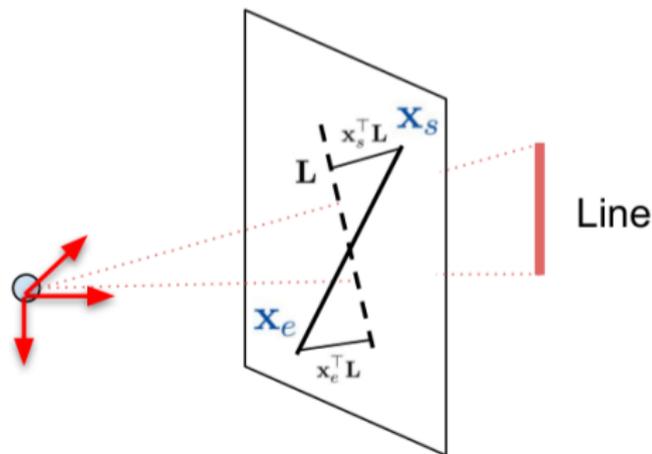
- State parameters:  $\mathbf{x} = \left[ \mathbf{x}_I^\top \quad \mathbf{x}_{calib}^\top \quad t_d \quad \mathbf{x}_c^\top \right]^\top$
- Perform online spatial and temporal calibration for both point&line features.
- Limit state vector size through MSCKF feature null-space operation.

# Line Measurement

- Camera line measurement:

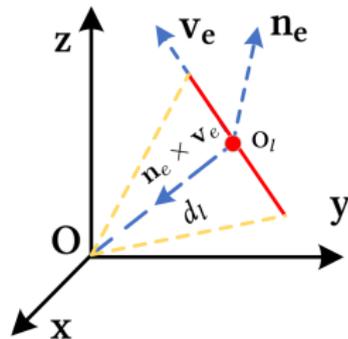
$$\mathbf{z}_l = \left[ \frac{\mathbf{x}_s^\top \mathbf{l}}{\sqrt{l_1^2 + l_2^2}} \quad \frac{\mathbf{x}_e^\top \mathbf{l}}{\sqrt{l_1^2 + l_2^2}} \right]^\top \quad (1)$$

- Start endpoint:  
 $\mathbf{x}_s = [u_s, v_s, 1]^\top$
- End endpoint:  
 $\mathbf{x}_e = [u_e, v_e, 1]^\top$
- Projected 2D image  
line:  $\mathbf{L}$



# Line Representation

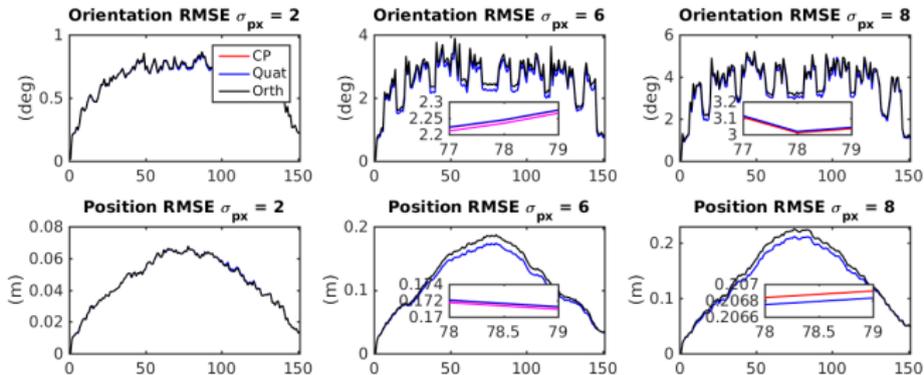
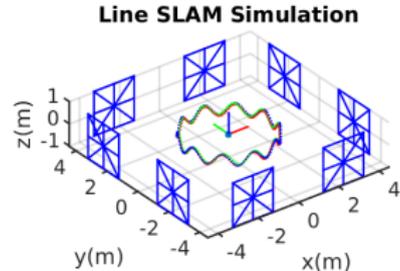
- The norm of plane formed by line with orig  $\mathbf{O}$ :  $\mathbf{n}_e$  .
- Line direction:  $\mathbf{v}_e$
- Line distance to orig  $\mathbf{O}$ :  $d_l$  .
- Orientation form  $\mathbf{R}(\bar{q}) = [\mathbf{n}_e, \mathbf{v}_e, \mathbf{n}_e \times \mathbf{v}_e]$ .



Model #	Line	Error states
Orthonormal	$\mathbf{n}_l, \mathbf{v}_l$	$\delta\theta_l, \delta\phi_l$
Quaternion	$d_l, \bar{q}_l$ with $\mathbf{R}(\bar{q}_l) = [\mathbf{n}_e, \mathbf{v}_e, \mathbf{n}_e \times \mathbf{v}_e]$	$\delta\theta_l, \tilde{d}_l$
Closest Point (CP)	$\mathbf{p}_l = d_l \bar{q}_l$	$\mathbf{p}_l = \hat{\mathbf{p}}_l + \tilde{\mathbf{p}}_l$

# Simulation: Line Representation Comparisons

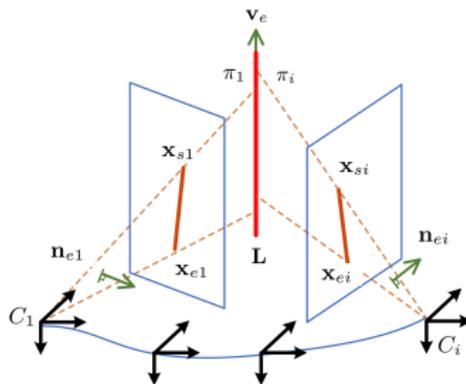
- Visual SLAM environment.
- Orthogonal, Quat and Closest Point (CP) line are compared.
- Finding: Quat and CP perform equally better than Ortho.



# Line Triangulation - Overview

Given series of line segment observations from different clones  
⇒ Estimate of geometric elements ( $\mathbf{n}_e$ ,  $\mathbf{v}_e$  and  $d_l$ ) of the 3D line.

- Algorithm A: based on orthogonality to formulate linear system to recover  $\mathbf{n}_e$ ,  $\mathbf{v}_e$  and  $d_l$  respectively.
- Algorithm B: based on two intersecting planes to formulate Plücker matrix which contains 3D line parameters.



# Line Triangulation - Algorithm A

Algorithm A:

- Recover  $\mathbf{n}_e$ :

$$C_1 \mathbf{n}_e = \frac{\mathbf{x}_{s1} \times \mathbf{x}_{e1}}{\|\mathbf{x}_{s1} \times \mathbf{x}_{e1}\|}$$

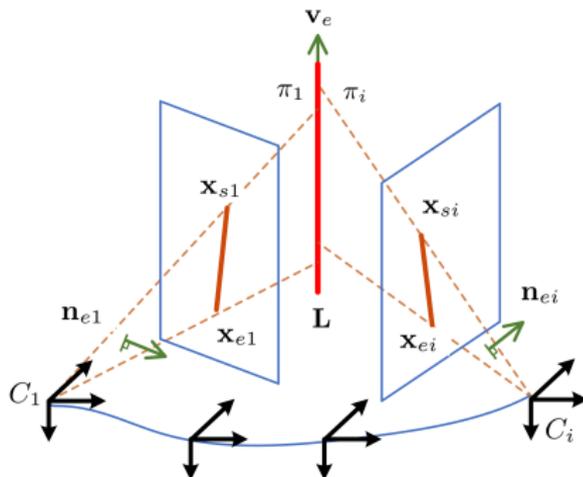
- Recover  $\mathbf{v}_e$ :

$$\begin{bmatrix} \vdots \\ C_i \mathbf{n}_{ei}^T C_1 \mathbf{R}^T \\ \vdots \end{bmatrix} C_1 \mathbf{v}_{e1} = \mathbf{0}$$

- Recover the line distance  $d_l$ :

$$\begin{bmatrix} \vdots \\ \mathbf{b}_i^T C_1 \mathbf{n}_{e1} \\ \vdots \end{bmatrix} C_1 d_l = \begin{bmatrix} \vdots \\ \mathbf{b}_i^T [C_1 \mathbf{p}_{C_i}] C_1 \mathbf{R}^{C_i} \mathbf{v}_{ei} \\ \vdots \end{bmatrix}$$

where  $\mathbf{b}_i = [C_1 \mathbf{v}_{e1}] C_1 \mathbf{R}^{C_i} \mathbf{n}_{ei}$ .



# Line Triangulation - Algorithm B

Algorithm B:

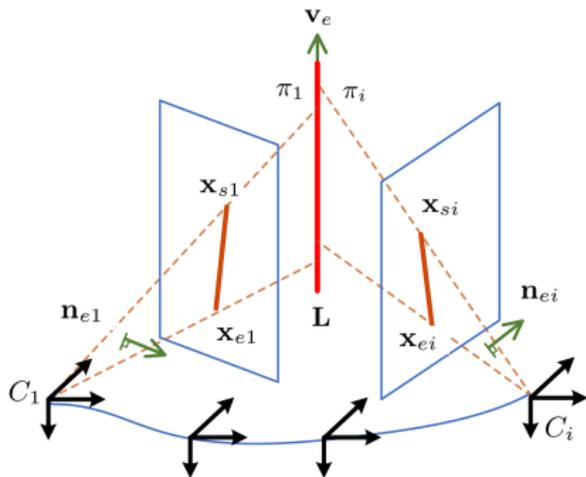
- The Plücker matrix:

$$\mathbf{L}^* = \pi_1 \pi_i^\top - \pi_i \pi_1^\top = \begin{bmatrix} [C_1 \mathbf{v}_{e1}] & C_1 d_l^{(i)} C_1 \mathbf{n}_{e1} \\ -C_1 d_l^{(i)} (C_1 \mathbf{n}_{e1})^\top & 0 \end{bmatrix}$$

- Recover geometry:

$$C_1 \mathbf{n}_{e1} = \sum_{i=2}^m C_1 \mathbf{n}_{e1}^{(i)} / \left\| \sum_{i=2}^m C_1 \mathbf{n}_{e1}^{(i)} \right\|$$

$$C_1 \mathbf{v}_{e1} = \sum_{i=2}^m C_1 \mathbf{v}_{e1}^{(i)} / \left\| \sum_{i=2}^m C_1 \mathbf{v}_{e1}^{(i)} \right\|$$

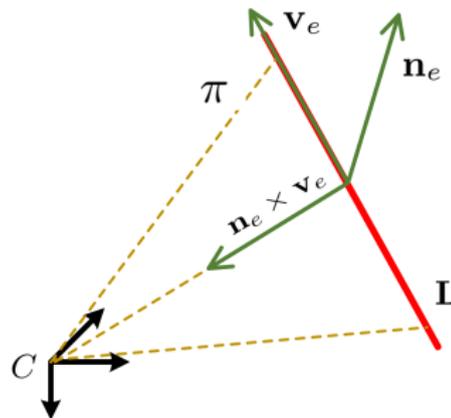


# Degenerate Motion

- Degenerate motions cause the line parameters to become unobservable, hence should be avoided.
- Any combined degenerate motions are also degenerate (i.e. all motions within the plane  $\pi$  will be degenerate).

**Table 1:** Degenerate Motion Summary

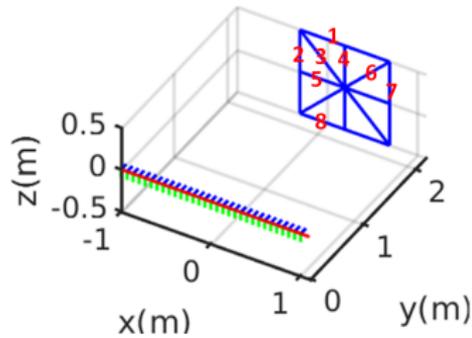
Motion	Solvable	Unsolvable
Along line direction: $\mathbf{v}_e$	$\mathbf{n}_e$	$\mathbf{v}_e$ and $d$
Toward line: $\mathbf{v}_e \times \mathbf{n}_e$	$\mathbf{n}_e$	$\mathbf{v}_e$ and $d$
Pure rotation	$\mathbf{n}_e$	$\mathbf{v}_e$ and $d$
Perpendicular to plane: $\mathbf{n}_e$	$\mathbf{n}_e, \mathbf{v}_e$ and $d$	-
Random motion	$\mathbf{n}_e, \mathbf{v}_e$ and $d$	-



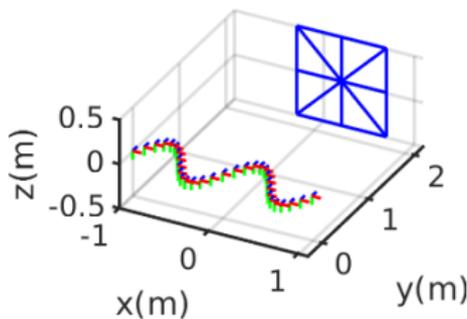
# Simulation: Triangulation Algorithm and Degenerate Motion

- Simulate 3 motions with 8 lines.
- Algorithm A&B are implemented.
- Lines 1,5&8 are degenerate in 1D motion.

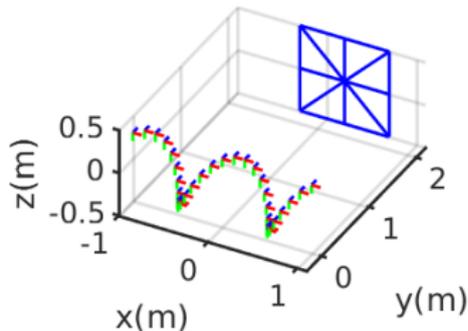
### 1D Motion with Lines



### 2D Motion with Lines

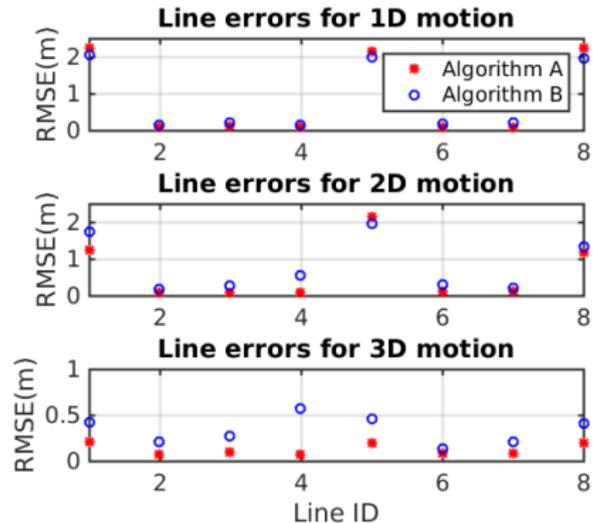
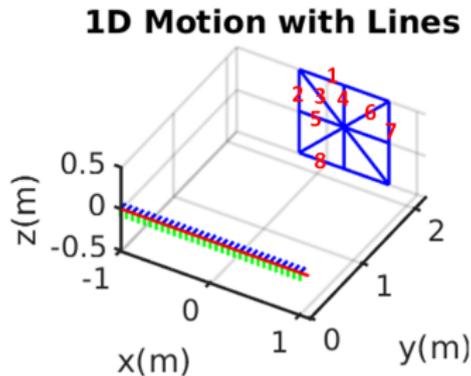


### 3D Motion with Lines



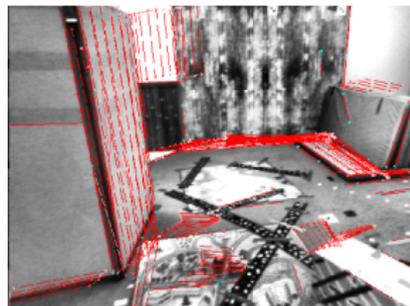
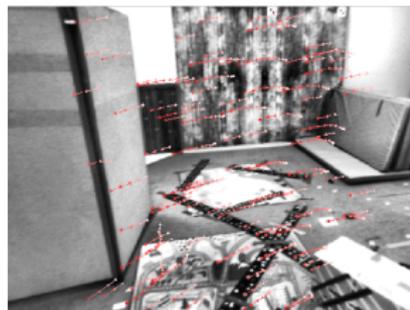
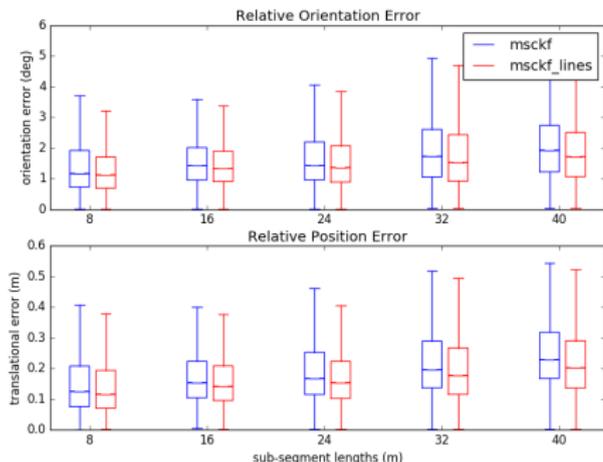
# Simulation: Triangulation Algorithm and Degenerate Motion

- Algorithm A, which takes advantage of the geometrical orthogonality, is better than B.
- Algorithm A w/ 3D motion performs best.



# Real-World Experiments: EuRoc Datasets Results

- Adding lines improves the overall accuracy in most cases.
- Line quality is affected by environment structure, mono camera motion and visual tracking.





## Visual-Inertial Odometry with Point and Line Features

Yulin Yang, Patrick Geneva,  
Kevin Eickenhoff and Guoquan Huang

Robot Perception and Navigation Group (RPNG)  
Department of Mechanical Engineering  
University of Delaware

### Visual Inertial Odometry with Point and Line Features

- A tightly-coupled mono-VIO with **point&line** features.
- Analysis different line triangulation algorithms and their **degenerate** motion.
- Compared **line representations** and showed Quat. and CP outperformed Ortho for larger pixel noises.
- Future work: Leverage SLAM line features (free&structural line), evaluate inverse depth line representations.

Y. Yang, P. Geneva, K. Eickenhoff, G. Huang  
{yuyang,pgeneva, keck, ghuang}@udel.edu