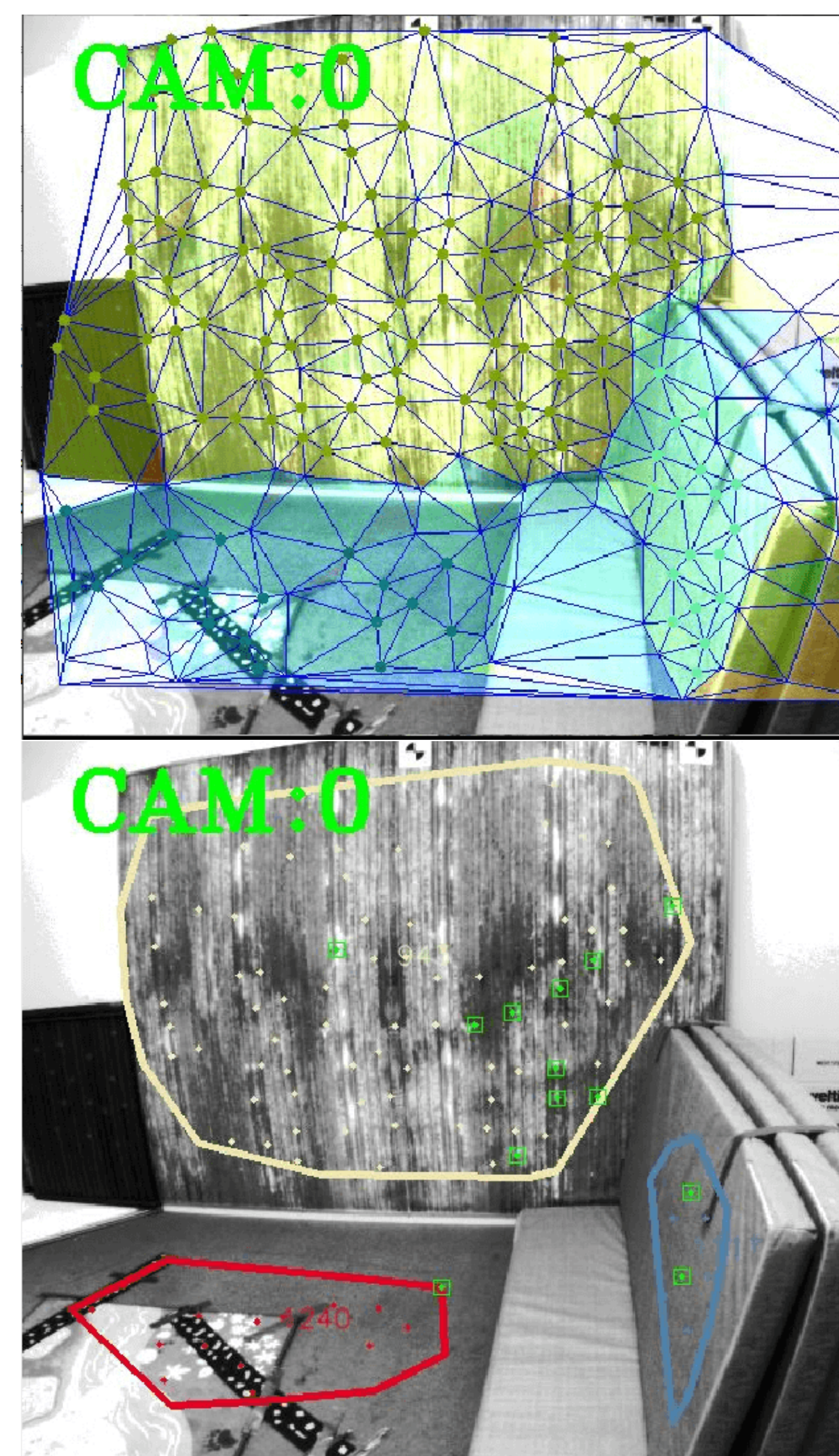


Motivation & Contribution

- Man-made environments have rich **structural** information (i.e. wall, ground, table and etc.)
- Regularization constraints can represent **higher-level, larger-spatial** geometric information and further improve state estimation
- **Contributions:**
 - **Monocular** filter-based VIO that enforces 3D feature **structural regularities** to environmental planes
 - A novel **robust** plane detection and tracking
 - **Open sourced** code and dataset for community

Plane Feature Detection and Tracking

- **Sparse Point Features**
 - FAST detect and KLT track
 - Enables temporal tracking
- **Point Feature Processing**
 - Recover 3D feature positions
 - Delaunay triangulation
 - Compute triangle normals
- **Vertex Normals**
 - Avg. normals for each vertex
 - Reject high variances ones
- **Vertex Matching Heuristics**
 - Pairwise match comparison
 - Robustly filter outliers



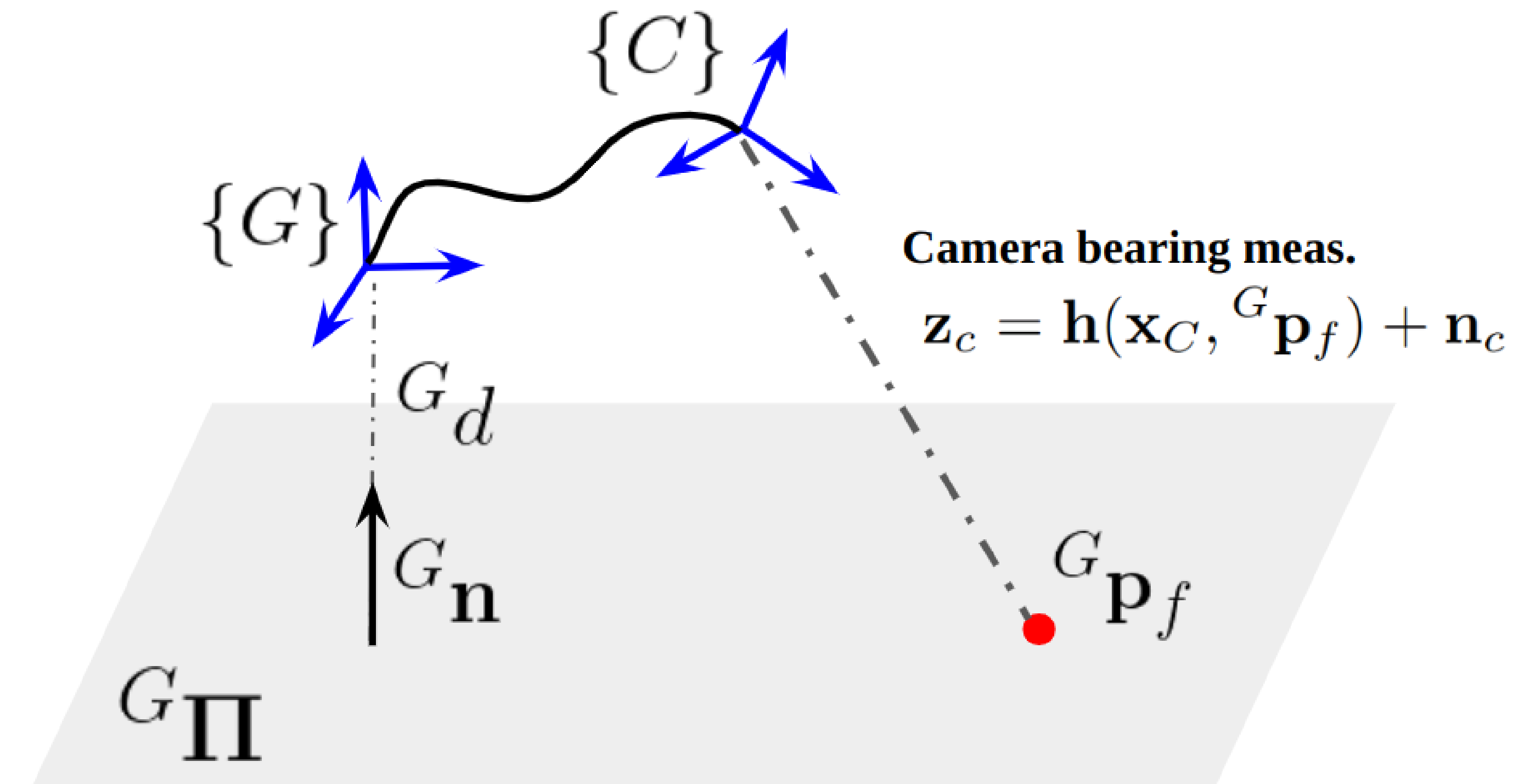
Results - Detection and Tracking

- Plane feature can be tracked longer than point features
- Feature tracking algorithm is **efficient** and **robust**

Table 1: Tacking statistics: number of point feature per plane, plane per frame, plane tracking length and active planes in the state per frame

Dataset	Feat. / PL	PL / Frame	Track Len.	PL Active	Time (ms)
table_01	27.3 ± 13.1	2.7 ± 1.1	61.1 ± 227.6	1.1 ± 0.5	3.5 ± 0.7
table_02	82.0 ± 58.7	2.2 ± 1.3	49.1 ± 249.2	1.2 ± 0.6	4.1 ± 0.9
table_03	33.9 ± 21.3	3.0 ± 1.2	88.5 ± 337.4	1.5 ± 0.6	4.0 ± 0.7
V1_01	19.6 ± 13.3	2.9 ± 1.3	53.4 ± 74.0	0.9 ± 0.7	3.3 ± 0.7
V1_02	13.7 ± 10.9	1.7 ± 1.3	20.0 ± 26.8	0.3 ± 0.5	2.5 ± 0.8
V1_03	10.1 ± 9.4	0.7 ± 1.0	24.9 ± 26.0	0.0 ± 0.2	2.0 ± 0.7

Plane-Aided VIO System Overview



Plane: $G_{\Pi} = G_n G_d$ Point: $G p_f$

• State Vector

$$\mathbf{x}_k = [\mathbf{x}_{I_k}^T \mathbf{x}_C^T \mathbf{x}_f^T \mathbf{x}_{\pi}^T]^T \quad \mathbf{x}_{I_k} = \begin{bmatrix} I_k^c \bar{q}^T G \mathbf{p}_{I_k}^T G \mathbf{v}_{I_k}^T \mathbf{b}_{g,k}^T \mathbf{b}_{a,k}^T \end{bmatrix}^T$$

$$\mathbf{x}_f = [G \mathbf{p}_{f_1}^T \dots G \mathbf{p}_{f_g}^T]^T \quad \mathbf{x}_{\pi} = [G \Pi_1^T \dots G \Pi_h^T]^T$$

• Point-on-Plane constraints

$$z_d = (G \mathbf{p}_f^T G \mathbf{n} - G_d) + n_d \quad (1)$$

• Regularity-constrained measurement

$$\begin{bmatrix} \tilde{z}_c \\ \tilde{z}_d \end{bmatrix} = \begin{bmatrix} \mathbf{H}_T^c \\ \mathbf{0} \end{bmatrix} \tilde{\mathbf{x}}_C + \begin{bmatrix} \mathbf{H}_f^c \\ \mathbf{H}_f^d \end{bmatrix} G \tilde{\mathbf{p}}_f + \begin{bmatrix} \mathbf{0} \\ \mathbf{H}_{\pi}^d \end{bmatrix} G \tilde{\Pi} + \begin{bmatrix} \mathbf{n}_c \\ n_d \end{bmatrix} \quad (2)$$

$$\Rightarrow \tilde{\mathbf{z}} = \mathbf{H}_T \tilde{\mathbf{x}}_C + \mathbf{H}_f G \tilde{\mathbf{p}}_f + \mathbf{H}_{\pi} G \tilde{\Pi} + \mathbf{n} \quad (3)$$

• Planar point feature update

- SLAM plane + SLAM point: Standard EKF update
- SLAM plane + MSCKF point

$$\tilde{\mathbf{z}} = \mathbf{H}_T \tilde{\mathbf{x}}_C + \mathbf{H}_f G \tilde{\mathbf{p}}_f + \mathbf{H}_{\pi} G \tilde{\Pi} + \mathbf{n} \quad (4)$$

- MSCKF plane + SLAM point:

$$\tilde{\mathbf{z}} = \mathbf{H}_T \tilde{\mathbf{x}}_C + \mathbf{H}_f G \tilde{\mathbf{p}}_f + \mathbf{H}_{\pi} G \tilde{\Pi} + \mathbf{n} \quad (5)$$

- MSCKF plane + MSCKF point:

$$\tilde{\mathbf{z}} = \mathbf{H}_T \tilde{\mathbf{x}}_T + \begin{bmatrix} \mathbf{H}_f & \mathbf{H}_{\pi} \end{bmatrix} \begin{bmatrix} G \tilde{\mathbf{p}}_f \\ G \tilde{\Pi} \end{bmatrix} + \mathbf{n} \quad (6)$$

Monte-Carlo Simulation

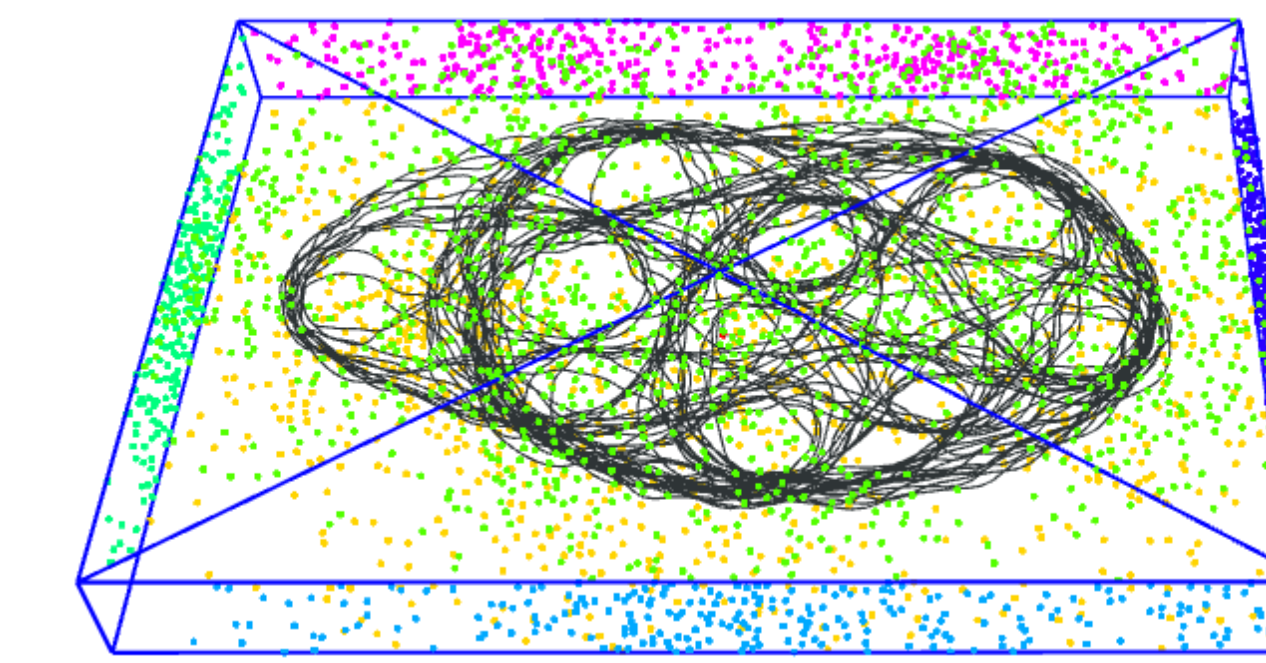


Table 2: Average 20 run RPE and NEEs for different algorithm configurations. Units are in degree / cm

Algorithm	60m	80m	100m	120m	NEES(3)
M-PT	0.37 / 4.3	0.44 / 5.0	0.50 / 5.6	0.55 / 6.2	3.39 / 1.75
M-PT & M-PL	0.37 / 4.3	0.43 / 4.9	0.48 / 5.5	0.53 / 6.1	3.34 / 1.72
M-PT & MS-PL	0.36 / 3.6	0.42 / 4.1	0.48 / 4.6	0.53 / 5.1	3.99 / 1.44
MS-PT	0.30 / 3.6	0.35 / 4.1	0.40 / 4.6	0.43 / 5.1	3.45 / 1.63
MS-PT & M-PL	0.29 / 3.5	0.33 / 4.0	0.37 / 4.5	0.41 / 4.9	3.09 / 1.44
MS-PT & MS-PL	0.29 / 2.9	0.35 / 3.3	0.39 / 3.7	0.42 / 4.1	3.38 / 1.20

- **M**: MSCKF features, **S**: SLAM features, **PT**: point, **PL**: plane.
- Extend OpenVINS [1] simulator to generate room walls and visual points lying on each plane
- Planar regularities **improve** state estimation and constrain both in-state and out-of-state features

Real-World Experiments

- Tested on released Indoor AR Table and EuRoC MAV datasets
- Planar regularities improve state estimation performance
- Plane detection and tracking is robust and efficient, tracking planes for significant periods of time
- The system is computationally cheap and efficient

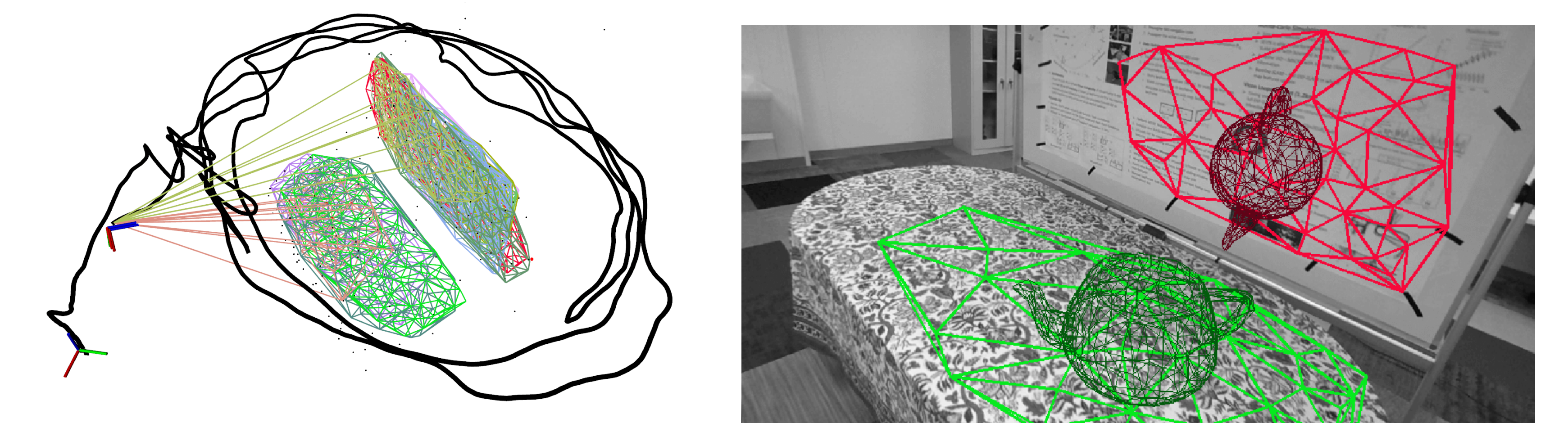



Table 3: ATE on self-collected Indoor AR Table and EuRoC MAV datasets (degree / cm). $n_d = 0.01$ was used.

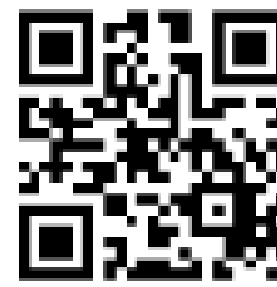
Algorithm	table_01	table_02	table_03	V1_01	V1_02	V1_03	Time (ms)
M-PT	0.45 / 6.8	0.85 / 2.4	1.37 / 5.6	0.83 / 8.6	1.57 / 9.1	2.50 / 15.5	8.7 ± 1.7
M-PT & M-PL	0.52 / 6.5	0.91 / 2.5	1.44 / 5.9	0.82 / 8.6	1.58 / 9.2	2.45 / 15.3	13.3 ± 3.2
M-PT & MS-PL	0.67 / 4.6	0.72 / 2.0	0.96 / 3.0	0.75 / 7.6	1.55 / 9.0	2.50 / 15.5	13.9 ± 2.9
MS-PT	1.15 / 5.7	1.79 / 4.1	2.41 / 6.9	1.32 / 8.4	1.58 / 7.0	2.20 / 12.2	9.4 ± 2.0
MS-PT & M-PL	1.32 / 5.5	0.89 / 2.5	1.03 / 4.5	0.61 / 5.3	1.58 / 7.5	2.32 / 12.5	15.0 ± 3.9
MS-PT & MS-PL	1.25 / 5.1	0.65 / 2.3	1.05 / 4.6	0.75 / 6.9	1.55 / 6.9	2.41 / 12.5	14.7 ± 3.2
VINS-Fusion [2]	1.62 / 5.8	1.32 / 3.0	1.47 / 7.6	1.24 / 5.8	2.61 / 11.5	3.61 / 20.5	35.6 ± 17.0*
OKVIS [3]	2.48 / 9.0	2.01 / 7.7	3.94 / 15.3	0.72 / 8.3	2.01 / 14.5	10.47 / 107.4	85.5 ± 32.6*

* Timing for VINS-Fusion [2] and OKVIS [3] only reports their optimization time (no feature tracking).

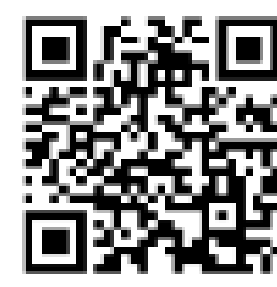
Explore Our Code and Dataset!



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Source Code



AR Table Dataset

[1] P. Geneva et al. "OpenVINS: A Research Platform for Visual-Inertial Estimation", ICRA, 2020. https://github.com/rpng/open_vins

[2] Qin et al. "VINS-Mono: A Robust and Versatile Monocular Visual-Inertial State Estimator", TRO, 2018.

[3] Leutenegger et al. "Keyframe-Based Visual-Inertial SLAM using Nonlinear Optimization", RSS, 2013.